



c) Evaluate:  $\iint_R x \sqrt{1-x^2} dx dy$ , where  $R: 0 \leq x \leq 1, 2 \leq y \leq 3$ . (04)

**Q-5**

**Attempt all questions** (14)

a) Evaluate  $\iint_R y dx dy$  where  $R$  is region bounded by the parabolas  $y^2 = 4x$  and  $x^2 = 4y$ . (05)

b) Evaluate  $\iint_R \sqrt{x+y} dx dy$ , where  $R$  is the parallelogram bounded by the lines  $x+y=0, x+y=1, 2x-3y=0, 2x-3y=4$ . (05)

c) Change the order of integration  $\int_0^{4a} \int_{x^2/4a}^{2\sqrt{ax}} dy dx$ . (04)

**Q-6**

**Attempt all questions** (14)

a) Verify Green's theorem for  $\int_c [(x-y)dx + 3xydy]$ , where  $c$  is the boundary of the region bounded by the parabolas  $x^2 = 4y$  and  $y^2 = 4x$ . (09)

b) Using Stoke's theorem for the vector field  $\vec{F} = (x+y)i + (y+z)j - xk$  and  $S$  is the surface of the plane  $2x+y+z=2$  which is in the first octant. (05)

**Q-7**

**Attempt all questions** (14)

a) Solve:  $p \tan x + q \tan y = \tan z$ . (05)

b) Solve:  $(mz - ny)p + (nx - lz)q = ly - mx$ . (05)

c) Form a partial differential equation by eliminating arbitrary constants from the equation  $z = a(x+y) + b$  where  $a, b$  are constants. (04)

**Q-8**

**Attempt all questions** (14)

a) Prove that radius of curvature for the curve  $y = f(x)$  is  $\frac{(1+y_1^2)^{3/2}}{y_2}$ . (05)

b) Find radius of curvature for the curve  $r = a(1 - \cos\theta)$ . (05)

c) Find the double points of the curve  $x^3 + y^3 - 12x - 27y + 70 = 0$  (04)

